School of Arts \& Science MATHEMATICS DEPARTMENT

## Algebra and Precalculus

Winter 2012

## COURSE OUTLINE

The course description is online @ http://camosun.ca/learn/calendar/current/web/math.html
$\Omega \quad$ Please note: the College electronically stores this outline for five (5) years only. It is strongly recommended you keep a copy of this outline with your academic records. You will need this outline for any future application/s for transfer credit/s to other colleges/universities.

## 1. Instructor Information

| (a) | Instructor: | Nick Marsden |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :---: |
| (b) | Office Hours: | Mon, Tue, Thu, Fri 10:30 to 11:30 plus usually also daily 11:30-2:30 |  |  |  |
| (c) | Location: | Ewing 258 |  |  |  |
| (d) | Phone: | $250-370-3499$ | Alternative Phone: |  |  |
| (e) | Email: | nmarsden@camosun.ca |  |  |  |
| (f) | Website: |  |  |  |  |

## 2. Intended Learning Outcomes

(No changes are to be made to these Intended Learning Outcomes as approved by the Education Council of Camosun College.)

Upon completion of this course the student will be able to:

1. Read and write mathematics at a level sufficient for entry into first year calculus.
2. Factor polynomials. Simplify rational expressions, complex fractions and radicals. Factor and simplify expressions with rational exponents.
3. Derive the quadratic formula. Choose efficient strategies to solve quadratic equations. Solve radical equations and equations involving rational expressions. Solve equations and inequalities involving absolute value. Solve problems involving direct, inverse and joint variation.
4. State the formulas for the slope - intercept and point - slope form of lines and use these formulas to find equations of lines. Graph linear equations and find equations from graphs. Model real-life problems with linear equations.
5. Recognize the equations of circles, ellipses, hyperbolas and parabolas. Write the equations of circles, ellipses and hyperbolas in standard form and graph these relations. Find the vertices of hyperbolas and ellipses. Find the equations of the asymptotes for hyperbolas. Solve linear and nonlinear systems of equations graphically and algebraically.
6. Define the term function. Determine if relations are functions. Find the domains of functions. Define even and odd functions and test functions to determine if they are even, odd or neither. Form and simplify difference quotients and explain their graphical interpretation and significance.
7. Identify the graphs of common algebraic functions. Evaluate and graph piecewise defined functions.
8. Construct algebraic functions to model simple real-life problems.
9. Translate verbal descriptions of transformations to function notation and vice versa. Interpret and graph multiple transformations of functions.
10. Analyze and graph quadratic functions. Solve optimization problems modelled with quadratic functions.
11. Graph polynomial functions using end behaviour and behaviour near their x-intercepts. Analyze graphs of polynomial functions and construct possible equations.
12. Graph rational functions using symmetry, asymptotes, behaviour near their x-intercepts and tables of signs. Analyze graphs of rational functions and construct possible equations.
13. Solve polynomial and rational inequalities.
14. State the Remainder, Factor and Rational Zeros Theorems and use these theorems to factor polynomials and find their real zeros.
15. Compose and decompose functions. State the definition of an inverse function. Verify that two functions are inverses using the definition. Find inverse functions algebraically and graphically.
16. Explain the relationship between exponential and logarithmic functions. Graph exponential and logarithmic functions and their transformations.
17. Prove the properties of logarithms and use these properties to simplify expressions and solve equations.
18. Solve applied problems involving pH , the Richter scale, decibels, compound interest, exponential growth, exponential decay and logistic growth.
19. Define a radian and work with radian measure. Convert between degree and radian measure.
20. State the unit circle definitions for the sine and cosine functions. Using the definitions, deduce properties of the sine and cosine functions and sketch their graphs. Graph transformations of these functions. Analyze sinusoidal graphs and construct possible equations. Model cyclical patterns, including temperature variation and height of tides.
21. Define the tangent, cotangent, secant and cosecant functions in terms of the sine and cosine functions. Graph the tangent, cotangent, secant and cosecant functions using the sine and cosine graphs.
22. State the right triangle definitions for the trigonometric functions. Use reference triangles to find exact values of trigonometric functions. Solve applied problems involving right triangles.
23. Derive the Pythagorean identities, the sum and difference identities, the double angle identities, the power reducing identities and the half angle identities. Use these identities to simplify expressions and verify other identities.
24. Graph the inverse sine, cosine and tangent functions. Find exact values for compositions of trigonometric and inverse trigonometric functions. Write compositions as algebraic expressions.
25. Find exact and approximate solutions of trigonometric equations, including equations involving identities and multiples of angles.
26. Identify patterns in sequences and write formulas for the general terms. Write the terms of recursively defined sequences. Express sums using summation notation. Simplify and evaluate basic sums of sequences.
27. Identify geometric sequences and series. Derive formulas for the nth terms of arithmetic and geometric sequences and for the sums of the first $n$ terms of these sequences. Solve word problems involving arithmetic and geometric sequences and series.
28. Expand binomials using Pascal's triangle.

## 3. Required Materials

(a) Texts: Sullivan, M. Algebra \& Trigonometry, $8^{\text {th }}$ edition
(b) Other

## 4. Course Content and Schedule

(This section can include: class hours, lab hours, out of class requirements and/or dates for quizzes, exams, lectures, labs, seminars, practicums, etc.)

## COURSE OUTLINE FOR MATH 105

Instructor: Nick Marsden, Ewing 258
Text: Sullivan, Algebra \& Trigonometry, 8th Edition, or The Custom Edition for Camosun College, first or second edition.

CHAPTER R: Review

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# Text Time
1 R. }42\mathrm{ Polynomials; Pascal's triangle
R. }52\mathrm{ Factoring Polynomials
3 R.7 2.5 Rational Expressions
4 R. }8\quad2.5\mathrm{ nth Roots; Rational Exponents
TAKE-HOME TEST
TEST 1, Lessons 1 to 4
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CHAPTER 1: Equations and Inequalities

| \# | Text | Time |
| :---: | :---: | :---: |
| 5 | 1.2 | 2 Quadratic Equations |
| 6 | 1.4 | 2 Radical Equations; Equations Quadratic in Form; Factorable Equations |
| 7 | 1.5,1.6 | 2 Solving Inequalities |

CHAPTER 2: Graphs
$8 \quad 2.1 \quad 1$ The Distance and Midpoint Formulas
92.21 Graphs of Equations in Two Variables; Intercepts; Symmetry
$10 \quad 2.3 \quad 1$ Lines
$11 \quad 2.4 \quad 1 \quad$ Circles
12 Notes 2 Systems of Equations TAKE-HOME TEST TEST 2, Lessons 5 to 12

CHAPTER 3: Functions and Their Graphs
\# Text Time
13 3.1-3.3 2 Review of Functions; Newton Quotients
$14 \quad 3.4 \quad 1$ Library of Functions; Piecewise-defined Functions
153.53 Graphing Techniques: Transformations; Conics

CHAPTER 4: Linear and Quadratic Functions

| \# | Text | Time |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 16 | 4.3 | 1 | Quadratic Functions and Their Properties |  |  |
| 17 | 4.4 | 1 | Quadratic Models |  |  |
|  |  | TAKE-HOME TEST |  |  |  |

CHAPTER 5: Polynomial and Rational Functions

| \# | Text | Time |  |
| :---: | :---: | :---: | :--- |
| 18 | 5.1 | 1 | Polynomial Functions of Higher Degree |
| 19 | 5.2 | 1 | Properties of Rational Functions |
| 20 | 5.3 | 1 | The Graph of a Rational Function |
| 21 | 5.4 | 1 | Polynomial and Rational Inequalities |
| 22 | 5.5 | 2 | The Real and Complex Zeros of a Polynomial Function |

CHAPTER 6: Exponential and Logarithmic Functions

| \# | Text | Time |  |
| :---: | :---: | :---: | :--- |
| 23 | 6.1 | 1 | Composite Functions |
| 24 | 6.2 | 1 | One-to-One Functions; Inverse Functions |
| 25 | 6.3 | 1 | Exponential Functions |
| 26 | 6.4 | 2 | Logarithmic Functions |
| 27 | 6.5 | 2 | Properties of Logarithms |
| 28 | 6.6 | 1 | Logarithmic and Exponential Equations |
| 29 | 6.7 | 1 | Compound Interest |
|  |  | TAKE-HOME TEST |  |
| 30 | 6.8 | Exponential Growth and Decay |  |
|  |  |  | TEST 4, Lessons 23 to 30 |

CHAPTER 7: Trigonometric Functions

| \# | Text | Time |  |
| :---: | :---: | :---: | :---: |
| 31 | 7.1 | 1 | Angles and Their Measure |
| 32 | 7.2 | 1 | Right Triangle Trigonometry |
| 33 | 7.4 | 2 Trigonometric Functions: the Unit Circle Approach |  |
| 34 | $7.6,7.8$ | Graphs of the Sine and Cosine Functions; Sinusoidal |  |
| 35 | 7.7 | Curve Fitting |  |
| 3 | Graphs of the Other Four Trigonometric Functions |  |  |

CHAPTER 8: Analytic Trigonometry
\# Text Time
36 8.1,8.2 2 The Inverse Sine, Cosine and Tangent Functions
$\begin{array}{llll}37 & 8.3 & 2 & \text { Trigonometric Identities }\end{array}$
TEST 5, Lessons 31 to 37
$38 \quad 8.4 \quad 2$ Sum and Difference Formulas
$39 \quad 8.5 \quad 2$ Double-angle and Half-angle Formulas
40 8.7,8.8 2 Trigonometric Equations
TAKE-HOME TEST
TEST 6, Lessons 31 to 40

CHAPTER 13: Sequences and Series

| \# | Text | Time |  |
| :---: | :---: | :---: | :---: |
| 41 | 13.1 | 1 | Sequences |
| 42 | 13.2 | 1 | Arithmetic Sequences |
| 43 | 13.3 | 2 | Geometric Sequences and Series |
|  |  | TEST 7, Lessons 41 to 43 |  |

## INTRODUCTION TO CALCULUS

| \# | Text | Time |  |
| :---: | :---: | :---: | :--- |
| C1 | Notes | 1 | Limits |
| C2 | Notes | 1 | The Secant line; Average Speed |
| C3 | Notes | 1 | The Tangent line; Instantaneous Speed |
| C4 | Notes | 1 | The Derivative Function |
| C5 | Notes | 2 | Differentiation Rules for Polynomials; Instantaneous |
|  |  | Speed |  |
| C6 | Notes | 1 Graphing Polynomial Functions |  |
| C7 | Notes | Max/Min Problems |  |
|  |  | TEST 8, Lessons 44 to C7 |  |

Review: 4 hours
Final exam

## 5. Basis of Student Assessment (Weighting)

(This section should be directly linked to the Intended Learning Outcomes.)

| (a) | Other <br> (eg, Attendance, <br> Project, Group <br> Work) | See below |
| :---: | :--- | :--- |
| (b) | Assignments | See below |
| (c) | Term tests | $50 \%$. Will throw out worse test if class participation and assignments are <br> satisfactory |
| (d) | Final exam | $50 \%$. or $100 \%$ if higher than term mark |

1. TERM MARK. You will be doing a number of take-home tests. These can be done in consultation with other students in your class, but with the help of nobody else. They will be overdue if not handed in at the beginning of the class on the due date, but can be handed in up to one day late with only a one mark deduction.

The term mark is the average of the scores on your in-class tests. However, if the average of your take-home test scores is at least 70\% AND your in-class participation is satisfactory, I will throw out your worst test before I calculate the average.

If you miss an in-class test for ANY reason, you will get a zero.
There will be no make-ups. But with decent take-home test scores and class participation, that zero will be tossed out.
2. FINAL EXAM. The final exam for this course is to be written by all students on the day and time scheduled.
3. MARK FOR THE COURSE. Your course mark is the larger of:
a) The average of your term percentage and your final exam percentage
b) Your final exam percentage

The Math Department reserves the right to raise your course mark if it is judged that your in-class tests and final exam were more difficult than those in other years or other sections.

## 6. Grading System

(No changes are to be made to this section unless the Approved Course Description has been forwarded through the Education Council of Camosun College for approval.)

## Standard Grading System (GPA)

| Percentage | Grade | Description | Grade Point Equivalency |
| :---: | :---: | :---: | :---: |
| 90-100 | A+ |  | 9 |
| 85-89 | A |  | 8 |
| 80-84 | A- |  | 7 |
| 77-79 | B+ |  | 6 |
| 73-76 | B |  | 5 |
| 70-72 | B- |  | 4 |
| 65-69 | C+ |  | 3 |
| 60-64 | C |  | 2 |
| 50-59 | D | Minimum level of achievement for which credit is granted; a course with a "D" grade cannot be used as a prerequisite. | 1 |
| 0-49 | F | Minimum level has not been achieved. | 0 |

## Temporary Grades

Temporary grades are assigned for specific circumstances and will convert to a final grade according to the grading scheme being used in the course. See Grading Policy E-1.5 at camosun.ca for information on conversion to final grades, and for additional information on student record and transcript notations.

| Temporary <br> Grade | Description |
| :---: | :--- |
| I | Incomplete: A temporary grade assigned when the requirements of a course have <br> not yet been completed due to hardship or extenuating circumstances, such as <br> illness or death in the family. |
| IP | In progress: A temporary grade assigned for courses that, due to design may <br> require a further enrollment in the same course. No more than two IP grades will be <br> assigned for the same course. (For these courses a final grade will be assigned to <br> either the 3 3d course attempt or at the point of course completion.) |
| CW | Compulsory Withdrawal: A temporary grade assigned by a Dean when an instructor, <br> after documenting the prescriptive strategies applied and consulting with peers, <br> deems that a student is unsafe to self or others and must be removed from the lab, <br> practicum, worksite, or field placement. |

7. Recommended Materials or Services to Assist Students to Succeed Throughout the Course

LEARNING SUPPORT AND SERVICES FOR STUDENTS

There are a variety of services available for students to assist them throughout their learning. This information is available in the College calendar, at Student Services, or the College web site at camosun.ca.

## STUDENT CONDUCT POLICY

There is a Student Conduct Policy which includes plagiarism.
It is the student's responsibility to become familiar with the content of this policy.
The policy is available in each School Administration Office, at Student Services, and the College web site in the Policy Section.

ADDITIONAL COMMENTS AS APPROPRIATE OR AS REQUIRED

