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\begin{array}{|c|c|}\hline & \begin{array}{c}\text { School of Arts \& Science } \\
\text { MATHEMATICS DEPARTMENT }\end{array}
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CAMOSUN \\

COLLEGE\end{array}\right]\)| MATH 189-X01 |
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|  |
| Technical Mathematics 3 |
| 2011 Q1 |

## COURSE OUTLINE

## 1. Instructor Information

| Instructor: | Raymond Lai |
| :--- | :--- |
| Office Hours: | Monday to Thursday: 10:30 am $-12: 20 \mathrm{pm}$ <br> By appointment |
| Office | CBA 152 |
| Phone: | $250-370-4491$ |
| Email: | lai@camosun.bc.ca |
| Website: | http://faculty.camosun.ca/raymondlai/ |

## 2. Course Description

Topics include: probability; frequency tables; probability distributions: discrete and continuous; curve fitting: linear regression, nonlinear regression; ordinary differential equations: first order, linear higher order, numerical methods.
Offered: Quarter 1 and Quarter 3
Credit: 3
In-Class Workload and Format: 5 hours of lecture/week for 11 weeks
Out-of-Class Workload: 5-10 hours/week (more for students with weak background)
Prerequisites: MATH 187 or MATH 175 or (MATH 101 and MATH 110).

## 3. Required Materials

Text:
(Optional) Washington, Allyn J., Basic Technical Mathematics with Calculus (Metric Version), 9th Edition, Addison-Wesley Publishing Company.
(Optional) Trushel, Peter J. and Chi-Ming Leung, Intermediate Statistics, Camosun College bookstore 2006.

Scientific calculator is required; graphing calculator (such as TI-89) is optional and is allowed in term tests and final examination (except in calculator-free sections, if any).

## 4. Intended Learning Outcomes

Upon completion of this course the student will be able to:

1. Use the Addition Rule and the Addition Rule for Non-disjoint Sets, the Multiplication Rule, factorials, permutations, and combinations in the statement and solution of counting problems.
2. Use the Addition Rule, Multiplication Rule, Contingency Tables, Probability Trees, and the Rules of Probability and of Conditional Probability to state and solve probability problems. Determine whether events are independent or dependent, and whether events are mutually exclusive.
3. Produce a stem and leaf plot, Pie Chart, Histogram, Frequency Polygon, Relative Frequency Polygon and Ogive for given data.
4. Find the Arithmetic Mean, Median, and Mode of raw data. Use the weighted mean formula to find the Arithmetic Mean. Use the probability formula $\bar{x}=\sum P(x) \cdot x$ to find the Arithmetic Mean of data represented in a frequency table.
5. Find the Population and Sample Variance and Standard Deviation of raw data, weighted data and data presented in a frequency table.
6. Apply the Empirical Rule or Tchebyshev's Theorem to make a table showing the expected percentage of scores, the actual number of scores, and actual percentage of scores which fall within one, two, and three standard deviations of the mean.
7. Use the Expected Value formula to find the Population and Sample Variance and Standard Deviation of weighted data, and of probability distributions. Determine the expected value in application problems.
8. Apply the Binomial Probability Formula to the solution of statistics problems. Determine the mean, variance, and standard deviation of any binomial distribution. Determine when the binomial distribution is appropriate for the solution of statistics problems.
9. Calculate the mean, variance, and standard deviation of the Poisson distribution. Solve problems involving the calculation of Poisson probabilities. Identify when it is appropriate to use the Poisson distribution as an approximation to the binomial distribution, and under appropriate conditions, use the Poisson distribution as an approximation to the binomial distribution.
10. Use the Standard Normal Table to solve standard normal problems. Use z-scores to compare results from distributions with different means and standard deviations. Use the Standard Normal Table to solve non-standard normal problems by converting them to standard normal problems.
11. Determine a point estimate for the mean. For given sample or population data, determine $90 \%, 95 \%$, and $99 \%$ confidence intervals for the mean. Use the Central Limit Theorem to estimate probabilities that means will be in certain intervals. Determine the size of a sample required for a given degree of confidence.
12. For given sample or population data, use standard chi-square tables to determine $90 \%$, $95 \%$, and $99 \%$ confidence intervals for the variance, and approximate confidence intervals for the standard deviation.
13. Determine a constant $k$ so that $y=k f(x)$ is a probability density function on the interval [ $c, d]$. Use the expected value formulas to find the mean, variance, and standard deviation of a given continuous probability distribution. Solve problems that involve calculating probabilities using continuous, uniform, and exponential distributions. Develop and use the formulas for the mean, variance, and standard deviation of the uniform and exponential distributions.
14. Given ( $x, y$ ) data points, determine the regression line (least squares line), and find and interpret the coefficients of correlation and determination.
15. Given ( $x, y$ ) data points, determine least squares curve of the form $y=a+b f(x)$ or of the form $y=B e^{k x}$. Use least squares to fit linear, quadratic, and cubic curves to given data points. Use regression curves to predict future results.
16. Use the techniques of Separation of Variables and Integrable Combinations to solve linear first order and first degree DEs. Use the Linear Differential Equation of First Order formula to solve linear first order and first degree DEs.
17. Solve second order linear constant coefficient homogeneous and non-homogeneous DE's. State and solve elementary application problems involving second order linear constant coefficient homogeneous and non-homogeneous DE's.
18. Use eigenvalues to solve Systems of Linear First-Order Differential Equations.
19. Recognize and solve the second-order Euler equation by the auxiliary equations method and by the eigenvalue method.
20. Use Euler's Method and the Runge-Kutta Method to approximate the solution to DEs by numerical methods.
21. Use calculators and computers for solving equations and using applications as noted above.

## 5. Course Content and Tentative Schedule

Differential Equations (20 hours) (Reference: Washington Sections 31.1-31.10)
Section 1 Solutions of Differential Equations
Section 2 Separation of Variables
Section 3 Integrating Combinations
Section 4 First Order Linear Differential Equations
Section $5 \quad$ Numerical Solution: Euler's Method and Runge-Kutta (RK4) Methods
Section 6 Applications of First Order Differential Equations
Section 7 Higher Order Homogeneous Linear Differential Equations
Section 8 Higher Order Nonhomogeneous Linear Differential Equations
Section 9 Applications of Higher Order Linear Differential Equations
Section 10 Cauchy-Euler Equation
Statistics and Probability (19 hours) (Reference: Trushel Sections 1-10, 13-18)
Section 11 Counting Techniques
Section 12 Introduction to Probability
Section 13 Introduction to Statistics
Section 14 Pictures of Data
Section 15 Measures of Central Tendency
Section 16 Measures of Variation
Section 17 Interpretation of Standard Deviation
Section 18 Expected Value
Section 19 Binomial Distribution
Section 20 Poisson Distribution
Section 21 Continuous Probability Density Functions
Section 22 Normal Distribution
Section 23 Estimate of Population Mean
Section 24 Estimate of Population Variance
Section 25 Linear Regression
Section 26 Non-Linear Regression

| Lecture | 39 hours |
| :--- | :--- |
| Tests | 3 hours |
| Leeway (including help sessions, reviews and holidays) | 13 hours |
| Total | 55 hours |

## 6. Basis of Student Assessment (Weighting)

To get a C or higher in the course, you must pass the final exam ( $50 \%$ or higher) *and* have an overall average of $60 \%$ or higher; your numerical grade will be computed using the following three components:

- 4 Assignments $(2.5 \% \times 4=10 \%)$
- due on 19 October, 9 November, 29 November, 7 December
- $50 \%$ penalty if turned in late
- marked solutions will be posted online at the class's website.
- 3 Tests
- tentatively on 27 October, 17 November, 2 December
- test 1 covers sections on assignment 1 , test 2 covers sections on assignment 2 , etc.
- some tests may have a calculator free section that does not allow use of calculator
- each test has an optional rewrite that will take place (most likely) outside regular class time (no other makeup is available)

If you rewrite a test, your grade for that test will be calculated using the formula

| $30 \%$ of your grade in the first trial + |
| :---: |
| $70 \%$ of the higher of your two grades in your first trial and the rewrite |

- Thorough understanding of the examples discussed in class and the homework exercises will be essential for success on the term tests.
- Solutions will be posted online at the class's website.
- Comprehensive Final Exam (50\%)
- during the week of $12 \mathrm{Dec}-16 \mathrm{Dec}$.
- As stated in the college calendar, "Students are expected to write tests and final examinations at the scheduled time and place. ... Exceptions, due to emergency circumstances, such as unavoidable employment commitments, health problems, or unavoidable family crisis, require approval of the appropriate instructor. Holidays or scheduled flights are not considered to be emergencies. The student may be required to provide verification of the emergency circumstances."
which is then converted to a letter grade using the standard Camosun grade scale (see Grading System (8) below).

There is one exception: if your term work is at least $50 \%$ *and* you received $60 \%$ or higher in the final exam, then you will receive a C in the course *even if* your overall average is under 60\%.

## 7. Course Policy

- Students are required to have their mobile phones either set on vibrate or turned off while attending class and writing term tests and final examination.
- Students are responsible for announcements made in class (check with your fellow students if you have to miss a class).

8. Grading System

Standard Grading System (GPA)

| Percentage | Grade | Description | Grade Point <br> Equivalency |
| :---: | :---: | :--- | :---: |
| $90-100$ | A+ |  | 9 |
| $85-89$ | A |  | 8 |
| $80-84$ | A- |  | 7 |
| $77-79$ | B+ |  | 6 |
| $73-76$ | B |  | 5 |
| $70-72$ | B- |  | 4 |
| $65-69$ | C+ |  | 3 |
| $60-64$ | C |  | 2 |
| $50-59$ | D |  | 1 |
| $0-49$ | F | Minimum level has not been achieved. | 0 |

## Temporary Grades

Temporary grades are assigned for specific circumstances and will convert to a final grade according to the grading scheme being used in the course. See Grading Policy at camosun.ca or information on conversion to final grades, and for additional information on student record and transcript notations.

| Temporary <br> Grade | Description |
| :---: | :--- |
| I | Incomplete: A temporary grade assigned when the requirements of a course have <br> not yet been completed due to hardship or extenuating circumstances, such as <br> illness or death in the family. |
| IP | In progress: A temporary grade assigned for courses that are designed to have an <br> anticipated enrollment that extends beyond one term. No more than two IP grades <br> will be assigned for the same course. |
| CW | Compulsory Withdrawal: A temporary grade assigned by a Dean when an <br> instructor, after documenting the prescriptive strategies applied and consulting with <br> peers, deems that a student is unsafe to self or others and must be removed from <br> the lab, practicum, worksite, or field placement. |

Temporary grades are assigned for specific circumstances and will convert to a final grade according to the grading scheme being used in the course. See Grading Policy E-1.5 at
camosun.ca for information on conversion to final grades, and for additional information on student record and transcript notations.

Note: A course with a "D" or "F" grade cannot be used as a prerequisite.

## 9. Recommended Materials or Services to Assist Students to Succeed Throughout the Course

## LEARNING SUPPORT AND SERVICES FOR STUDENTS

There are a variety of services available for students to assist them throughout their learning. This information is available in the College calendar, at Student Services or the College web site at camosun.ca.

## STUDENT CONDUCT POLICY

There is a Student Conduct Policy which includes plagiarism. It is the student's responsibility to become familiar with the content of this policy. The policy is available in each School Administration Office, at Student Services and on the College web site in the Policy Section.

How to do well in the course and where to get help

1. Do not skip classes. There will be problem solving techniques discussed in class not covered in the assignments.
2. Start working on the exercises as soon as we finish a section. Studying in groups is an efficient way to learn mathematics; however, make sure you can solve problems yourself.
3. It is important to understand the principles involved rather than to memorize a method of solution - try variations of questions.
4. Extra help available from assistant at the Math Lab located at Technologies Centre (TEC) Room 142 (phone: 370-4492). This drop-in centre is freely available for your use to work on math homework and to seek help from the tutor on staff (see hours posted on door).

Tentative Schedule

| Week (Dates) | Monday (1 hr) | Tuesday (2 hrs) | Wednesday (1 hr) | Thursday (1 hr) |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} 1 \\ (26 / 9 / 11-30 / 9 / 11) \end{gathered}$ | 26-Sept Section 1 | $\begin{aligned} & \text { 27-Sept } \\ & \quad \text { Sections } 2 \& 3 \end{aligned}$ | 28-Sept Section 3 | 29-Sept <br> Section 4 |
| $\begin{gathered} 2 \\ (3 / 10 / 11-7 / 10 / 11) \end{gathered}$ | 3-Oct <br> Section 4 | 4-Oct <br> Section 5 | 5-Oct <br> Section 6 | $\text { 6-Oct } \begin{aligned} & \text { Section } 6 \end{aligned}$ |
| $\begin{gathered} 3 \\ (10 / 10 / 11-14 / 10 / 11) \end{gathered}$ | $\begin{array}{\|l\|} \hline 10-\text { Oct } \\ \text { No Class } \\ \text { (Thanksgiving) } \end{array}$ | $\begin{aligned} & \text { 11-Oct } \\ & \text { Section } 6 \end{aligned}$ | $\begin{aligned} & \text { 12-Oct } \\ & \text { Section } 6 \end{aligned}$ | $\begin{aligned} & \text { 13-Oct } \\ & \text { Section } 7 \end{aligned}$ |
| $\begin{gathered} 4 \\ (17 / 10 / 11-21 / 10 / 11) \\ \hline \end{gathered}$ | $\begin{aligned} & \text { 17-Oct } \\ & \quad \text { Section } 7 \end{aligned}$ | $\begin{aligned} & \text { 18-Oct } \\ & \text { (Hw } 1 \text { Help Session) } \end{aligned}$ | $\begin{array}{\|c} \hline \text { 19-Oct } \\ \begin{array}{l} \text { Sections } 7 \& 8 \\ \text { (Hw } 1 \text { due) } \end{array} \\ \hline \end{array}$ | ${ }^{20-O c t} \text { Section } 8$ |
| $\begin{gathered} 5 \\ (24 / 10 / 11-28 / 10 / 11) \end{gathered}$ | 24-Oct <br> Section 8 | $\begin{aligned} & \text { 25-Oct } \\ & \text { Section 9, } \\ & \text { Test } 1 \text { Review } \end{aligned}$ | 26-Oct <br> Test 1 | 27-Oct <br> Sections 9 \& 10 |
| $\begin{gathered} 6 \\ (31 / 10 / 11-4 / 11 / 11) \end{gathered}$ | 31-Oct <br> Section 11 | $\text { 1-Nov } \begin{aligned} \\ \text { Section } 11 \end{aligned}$ | 2-Nov Section 12 | 3-Nov <br> Section 12 |
| $\begin{gathered} 7 \\ (7 / 11 / 11-11 / 11 / 11) \\ \hline \end{gathered}$ | 7-Nov <br> Section 13 | 8-Nov <br> (Hw 2 Help Session) | 9-Nov <br> Section 14 <br> (Hw 2 due) | 10-Nov Section 15 |
| $\begin{gathered} 8 \\ (14 / 11 / 11-18 / 11 / 11) \end{gathered}$ | 14-Nov <br> Section 16 | $\begin{aligned} & \text { 15-Nov } \\ & \text { Section 17, } \\ & \text { Test } 2 \text { Review } \end{aligned}$ | 16-Nov <br> Test 2 | 17-Nov <br> Section 18 |
| $\begin{gathered} 9 \\ (21 / 11 / 11-25 / 11 / 11) \\ \hline \end{gathered}$ | $\begin{aligned} & \text { 21-Nov } \\ & \text { Section } 19 \end{aligned}$ | $\begin{array}{\|l\|} \hline 22-\text { Nov } \\ \text { Sections } 19,20 \& 21 \end{array}$ | $\begin{aligned} & \text { 23-Nov } \\ & \text { Sections } 21 \& 22 \end{aligned}$ | 24-Nov <br> Sections 22 \& 23 |
| $\begin{gathered} 10 \\ (28 / 11 / 11-2 / 12 / 11) \end{gathered}$ | 28-Nov <br> (Hw 3 Help Session) | 29-Nov <br> Sections 24 \& 25 <br> (Hw 3 due) | $\begin{aligned} & \text { 30-Nov } \\ & \text { Test } 3 \text { Review } \end{aligned}$ | 1-Dec <br> Test 3 |
| $\begin{gathered} 11 \\ (5 / 12 / 11-9 / 12 / 11) \end{gathered}$ | 5-Dec <br> Section 26 | 6-Dec <br> (Hw 3 Help Session) | 7-Dec <br> Final Review <br> (Hw 4 due) | 8-Dec <br> Final Review |
| $\begin{gathered} 12 \\ (12 / 12 / 11-16 / 12 / 11) \end{gathered}$ | $\begin{array}{\|l\|} \text { 12-Dec } \\ \text { Exam Week } \end{array}$ | $\begin{aligned} & \text { 13-Dec } \\ & \text { Exam Week } \end{aligned}$ | $\begin{aligned} & \text { 14-Dec } \\ & \text { Exam Week } \end{aligned}$ | $\begin{aligned} & \text { 15-Dec } \\ & \quad \text { Exam Week } \end{aligned}$ |

